# Bayesian detection and uncertainty quantification of the first change point of the COVID-19 case curve in the Midwest: Timeliness of non-pharmaceutical interventions

Alessandro Maria Selvitella <sup>1</sup>

Kathleen Lois Foster<sup>2</sup>

<sup>1</sup>Purdue University Fort Wayne

<sup>2</sup>Ball State University

### 1. Introduction

#### Motivation.

The first case of COVID-19 was identified in Wuhan, China, after which it spread throughout Europe and the US, leading to an ongoing pandemic, as officially determined by WHO in March 2020. Since the very first stages of the pandemic, the global research community mobilized and started to study the evolution of COVID-19 to understand its virology, pathophysiology, and epidemiology. The complexity of the problem requires the development of new methodologies and the collaboration of large interdisciplinary teams.

#### Our Effort.

Our team joins this interdisciplinary research effort with the interest of understanding the dynamics of the disease from a machine learning perspective. We want to understand the time evolution of COVID-19 and in particular its changes with respect to non-pharmaceutical interventions (eg. lockdowns, social distancing, face mask, stay at home, and many others). In this poster, we will concentrate on understanding the relationship between qualitative changes in the curve of COVID-19 cases and two government policy orders: "Face Mask" and "Stay at Home".

# 5. Our Analysis

We ran the algorithm described in the methods with K=9000 iterations and 3 chains to estimate the parameter  $\psi$ . Our outcome variable Y is taken on the log scale and represents the natural logarithm of the cumulative case counts. We will have one Y for each of the twelve states in the Midwest. We estimated the posterior distribution of the change point parameter  $\psi$ , computed its posterior mean and its corresponding 95% credible interval for each of the twelve states in the Midwest. We compared this with the dates of the first case detected in each state and the dates of the "Stay at Home" and "Face Mask" orders. We performed the Savage-Dickey density ratio test to make this comparison.

State	Illinois	Indiana	lowa	Kansas	Michigan	Minnesota
First Case	24-01	06-03	08-03	08-03	10-03	06-03
Stay at Home	21-03	25-03	NO	30-03	24-03	28-03
Mask	01-05	27-07	16-11	03-07	27-04	24-07
First CP	28-02	07-04	29-04	11-04	01-04	27-04
LB CI	22-03	06-04	27-04	10-04	31-03	21-04
UB CI	23-04	08-04	01-05	14-04	02-04	02-05
State	Missouri	Nebraska	North Dakota	Ohio	South Dakota	Wisconsin
First Case	07-03	06-03	12-03	10-03	10-03	03-03
Stay at Home	06-04	NO	NO	24-03	NO	25-03
Mask	NO	04-05	14-11	23-07	NO	01-08
First CP	04-04	02-05	14-04	06-04	21-04	01-04
LB CP	03-04	30-04	10-04	04-04	19-04	03-04
UB CP	05-04	04-05	18-04	07-04	23-04	05-04

Table 1:This table provides the dd-mm-2020 dates for all 12 Midwest states for: First Case of COVID-19 (Row 1) , Stay at Home order (Row 2), Face Mask order (Row 3), First Change Point (CP)  $\psi$  (Row 4), Date of the Lower Bound (LB) of the 95% Credible Interval (CI) for  $\psi$  (Row 5), Date of the Upper Bound (UB) for the 95% CI for  $\psi$  (Row 6). NO indicates when an order was not executed.

## 2. Dataset and Software

- The case counts by state were taken from CDC, beginning with the first case in Washington reported on January 22, 2020 until February 21, 2021. The state policies, including dates and information on the "Stay at Home" and "Face Mask" orders, were taken from the COVID-19 US State Policy Database (CUSP) curated by Boston University.
- The analysis was performed using the software R and its packages mcp and patchwork.
- All data is publicly available and code is available upon request.

# 3. Bayesian Change Point Estimation

To estimate the change point we will use a Bayesian perspective. Although, the methodology can be adapted to multiple change points, we will concentrate on the case of one single change point. Consider a sequence of observations of an outcome variable Y (in our case the COVID-19 case counts), given by  $y_1,\ldots,y_T$  with T>0 the time extension of our study (January, 22nd 2020 to February 21st, 2021) and  $t=1,\ldots,T$  the corresponding time component. We model the mean response  $\mu=E[Y]$  with a piece-wise linear function such as  $\beta_1 t + \beta_2 (t-\psi)_+$ , where  $(t-\psi)_+:=(t-\psi)\,I\,(t>\psi)$  and  $I(\cdot)$  representing the indicator function. Here  $\beta_1$  is the slope at the left of the change point  $\psi$  and  $\beta_2$  is the difference-in-slopes between the slopes at left and right sides of  $\psi$ .

We will estimate change points and their level of uncertainty with the mean and standard deviation of their posterior distribution via **Monte Carlo Markov Chain** methods. The priors of all parameters are uninformative, with the exception of the prior for the change point which is restricted to be ordered monotonically while otherwise remaining uninformative.

# 3. Savage-Dickey Ratio Test

Suppose you observe data D and have the vector of parameters  $\theta=(\theta_1,\theta_2)$  with  $\theta_1$  the parameters of interest, and  $\theta_2$  nuisance parameters. Consider a null hypothesis,  $H_0:\theta_1=h$ , with h a fixed vector of hypothesized values of  $\theta_1$ . The alternative hypothesis is  $H_1:\theta_1\neq h$ . Denote  $p_0$  and  $p_1$  the probability density distributions under  $H_0$  and  $H_1$ , respectively. Suppose that  $\lim_{\theta_1\to h} p_1(\theta_2|\theta_1) = p_0(\theta_2)$ , then  $p_1(\theta_2|\theta_1=h) = p_0(\theta_2)$ . Consider the Bayes factor

$$BF_{01} := p(D|H_0)/p(D|H_1) = p_0(D)/p_1(D).$$

Ther

$$p_0(D) = \int p_0(D|\theta_2)p_0(\theta_2)d\theta_2 = \int p_1(D|\theta_2, \theta_1 = h)p_1(\theta_2|\theta_1 = h)d\theta_2 = p_1(D|\theta_1 = h),$$

which by Bayes' rule leads to

$$p_0(D) = \frac{p_1(\theta_1 = h|D)p_1(D)}{p_1(\theta_1 = h)}.$$

In this way, we obtain the **Savage-Dickey density ratio**, namely the ratio between posterior and prior distributions:

$$BF_{01} = \frac{p_0(D)}{p_1(D)} = \frac{p_1(\theta_1 = h|D)}{p_1(\theta_1 = h)}.$$

In our case, we are interested in the parameter  $\theta_1=\psi$ , the change point, although other parameters (eg. the two intercepts and two slopes) will be estimated as well. The observed data is  $D=\{(t,y_t)\}_{t=1}^T$ . Note also that the hypothesis we are interested in is actually one sided  $H_0: \psi > h_i$  with i=1,2. In particular, we want to test if the change point  $\psi$  arrives after the "Stay at Home" order  $h_1$  or not, and if it arrives after the "Face Mask" order  $h_2$  or not.

### 6. Results and Discussion

Figure 1 illustrates the results of the Bayesian Change Point Analysis with comparison to the dates of the "Stay at Home" (Red Bar) and "Face Mask" (Blue Bar) orders for each of the 12 states in the Midwest.

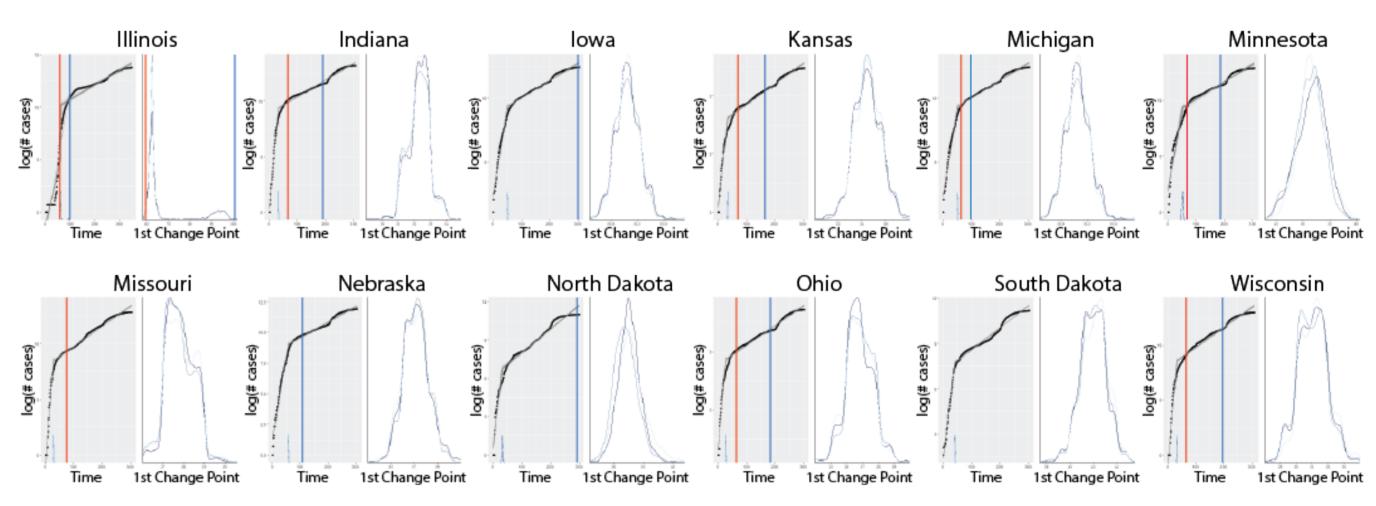


Figure 1:Left Plots: The horizontal axis represents the time variable, while the vertical represents the logarithm of the cumulative number of cases. Right Plots: Represents the posterior distribution of the first change point  $\psi$ .

- Illinois is the only state where we cannot exclude the possibility that the first change point is subsequent to the "Stay at Home" order. Note that Illinois saw the first case much earlier than the other states and registered a plateau soon after. Possibly related: Chicago is the biggest airline hub in the Midwest area by far, a fact that speculatively might be responsible for this impetus for the earlier crackdown on mask use and movement outside the home. The higher uncertainty of the estimate of the first change point in Illinois is possibly due to this plateau occurring at the beginning of the epidemic.
- The change points of Indiana, Kansas, Michigan, Minnesota, Ohio, and Wisconsin have been estimated to be before both governmental policies were put in place.
- Iowa and North Dakota did not execute a "Stay at Home" order, while the "Face Mask" order arrived much later than the estimated first change point.
- Missouri's policy recommended rather than required mask use, while its "Stay at Home" order was much later than the change point.
- Nebraska did not have a "Stay at Home" order and they mandated face mask use by employees only in public-facing businesses, and the first change point arrived before that.
- In South Dakota, there hasn't been any "Stay at Home" order, while masks were encouraged, but not required.

Altogether our results suggest that important government non-pharmaceutical interventions restricting movement outside the home and mandating the use of masks were put in place after a qualitative change in the COVID-19 case trajectory had already taken place. Thus, these government mandated policies were not a likely contributor to the observed first flattening in the curve of COVID-19 cases.

#### Conclusions

We studied the problem of detecting the first change point in the curve of COVID-19 cases in the twelve Midwest states. We found evidence that there has been qualitative rate changes in the diffusion of COVID-19 before the "Stay at Home" and "Face Mask" orders were implemented, in all states but Illinois. This calls for possibly quicker governmental actions. The analysis described in this manuscript is descriptive and not predictive, associative and not causal.